

List of selected formulae

Present values of annuities-certain:

$$\begin{aligned}\ddot{a}_{\overline{n}|} &= \frac{1-v^n}{1-v} & a_{\overline{n}|} &= v\ddot{a}_{\overline{n}|} \\ \ddot{a}_{\overline{n}|}^{(p)} &= \frac{1}{p} \left[\frac{1-v^n}{1-v^{\frac{1}{p}}} \right] & a_{\overline{n}|}^{(p)} &= v^{\frac{1}{p}} \ddot{a}_{\overline{n}|}^{(p)}.\end{aligned}$$

Expected present values of life annuities:

$$\begin{aligned}\ddot{a}_x &= \frac{N_x}{D_x} & \ddot{a}_{x:\overline{n}|} &= \frac{N_x - N_{x+n}}{D_x} & a_x &= \ddot{a}_x - 1 \\ \ddot{a}_x^{(p)} &\approx \ddot{a}_x - \frac{p-1}{2p} & a_x^{(p)} &\approx a_x + \frac{p-1}{2p} & a_x^{(p)} &= \ddot{a}_x^{(p)} - \frac{1}{p}\end{aligned}$$

Conversion relationships:

$$\begin{aligned}\bar{A}_x &= 1 - \delta \bar{a}_x \\ A_x &= 1 - d \ddot{a}_x \\ A_x^{(p)} &= 1 - d^{(p)} \ddot{a}_x^{(p)} \\ A_{x:\overline{n}|}^{(p)} &= 1 - d^{(p)} \ddot{a}_{x:\overline{n}|}^{(p)}\end{aligned}$$